

Channel Encoding & Decoding

Viterbi Algorithm

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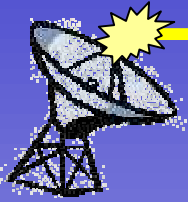
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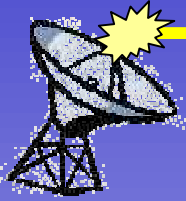
Channel Encoding & Decoding



1. Digital Communication System
2. Viterbi Algorithm
3. Advantages of the Viterbi Algorithm
4. Presentation of a Demonstration Software

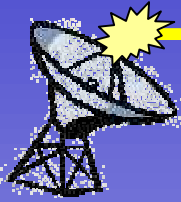
1. Digital communication system

- Definition of Viterbi algorithm
- Historical background of viterbi-coding
- Parts of a digital communication system
- Use of the Viterbi algorithm

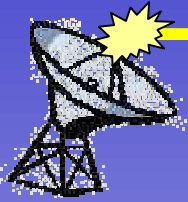


Digital communication system

- Problem of digital communication
 - Transmit much data via a noisy channel
 - Detect and correct errors
- Solution
 - Convolutional coding with
 - Forward error correction (FER)



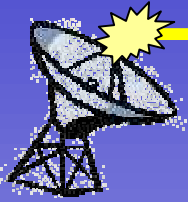
Viterbi Algorithm



The Viterbi-Algorithm is a basic part of the coding and modulation method of the digital data transmission.

With the help of the Viterbi-algorithm it is possible to recognise data errors and correct them at the receiver. [9]

Viterbi Algorithm



"...efficient methode of optimum sequence estimation of a finite-state process".

„finding the shortest path through a weighted graph“

Development

< 1955

Channel Encoding was implemented by

- Block codes
- Linear block codes

1955

Elias P. introduced

- Convolutional codes
- Fixed decoding time
- First real-time coding



Development

1967

Andrew J. Viterbi

- Founder of Qualcomm Corporation
- Developed the Viterbi Algorithm

...

Other researchers improved the channel coding methods

- Found new convolutional codes
- Improved the performance limits
- Designed implementations in hard- & software



Development

1993

Turbo coding merged

- Parallel concatenated convolutional technique
- Improves performance by chaining up:
Viterbi decoder and Reed-Solomon decoder
(data recycle through the decoder several times)

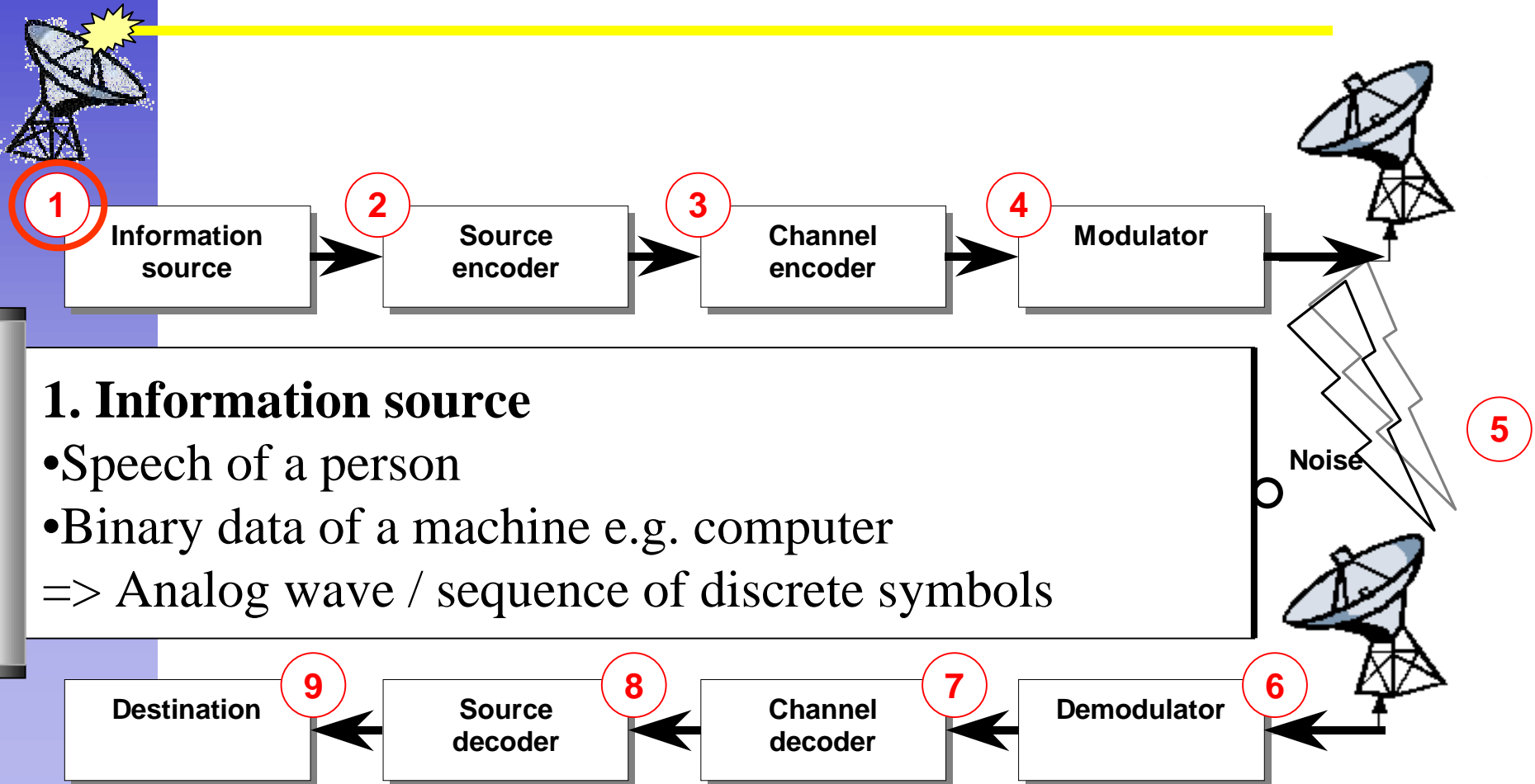
1995

Viterbi & Reed-Solomon decoding

- Used in space communication
- geostationary satellite communication



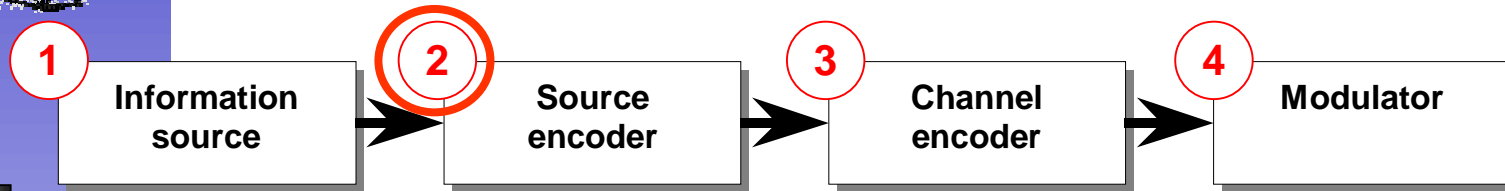
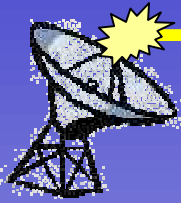
Digital communication system



1. Information source

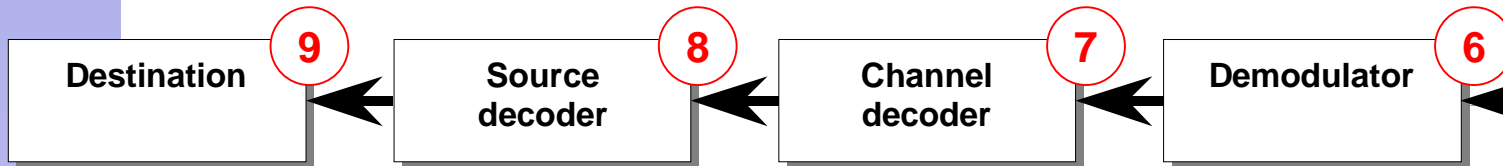
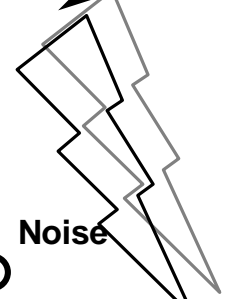
- Speech of a person
 - Binary data of a machine e.g. computer
- => Analog wave / sequence of discrete symbols

Digital communication system

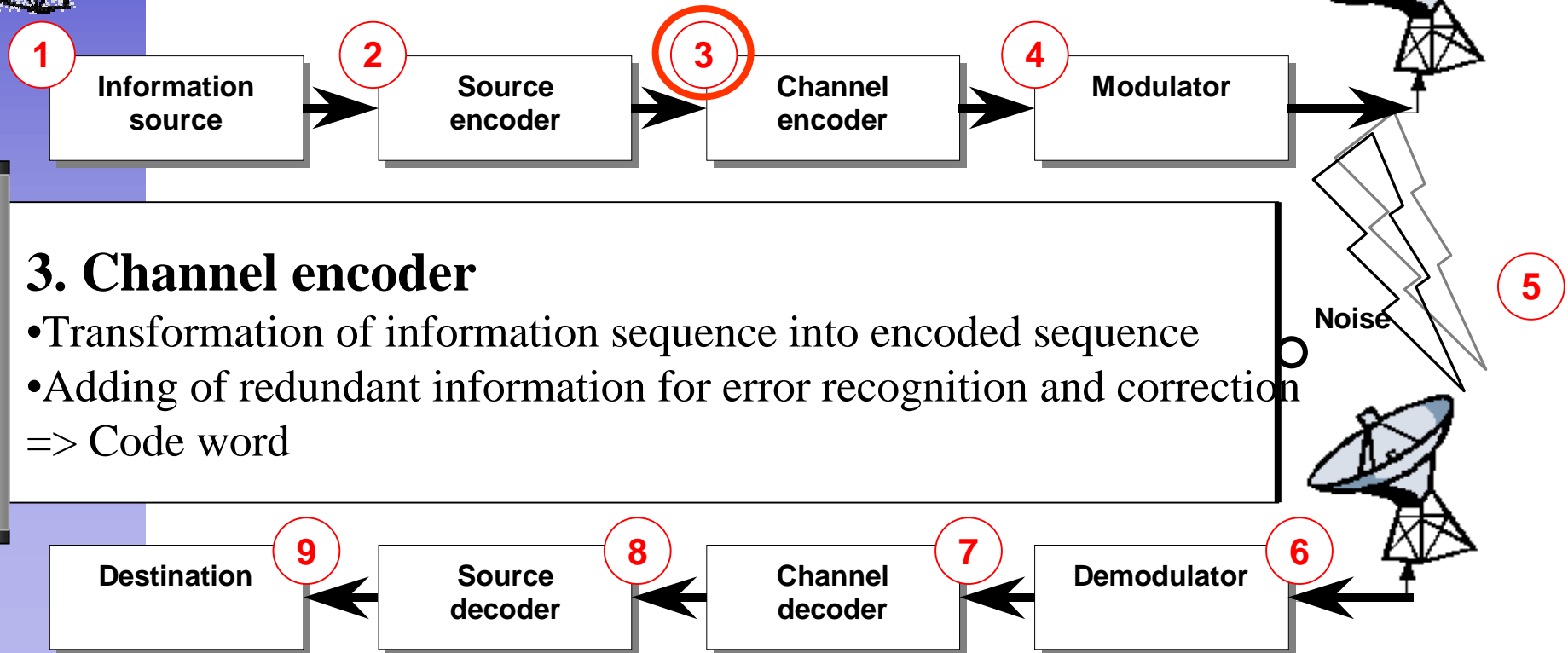
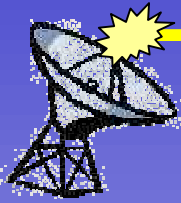


2. Source encoder (A/D converter)

- Transformation of analogue signal into digital signal
 - Compression of signal
- ⇒ Information sequence



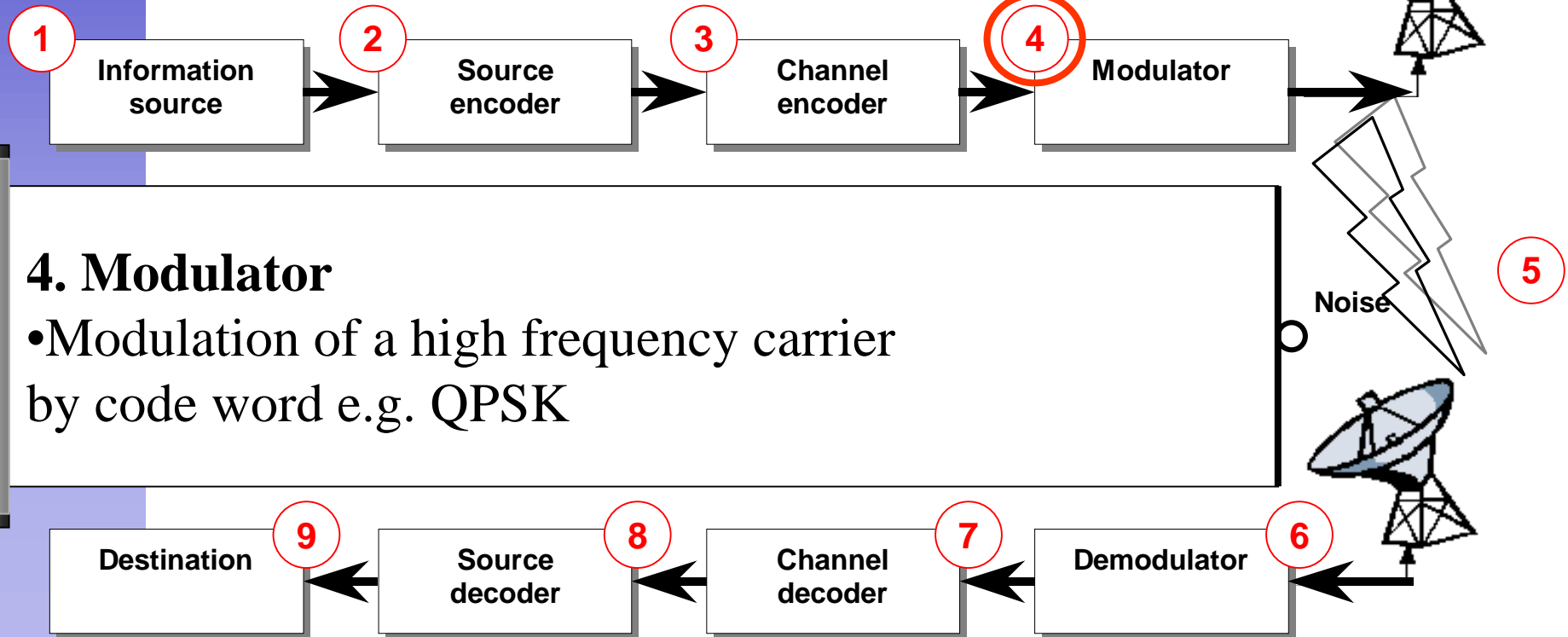
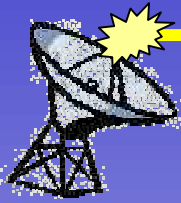
Digital communication system



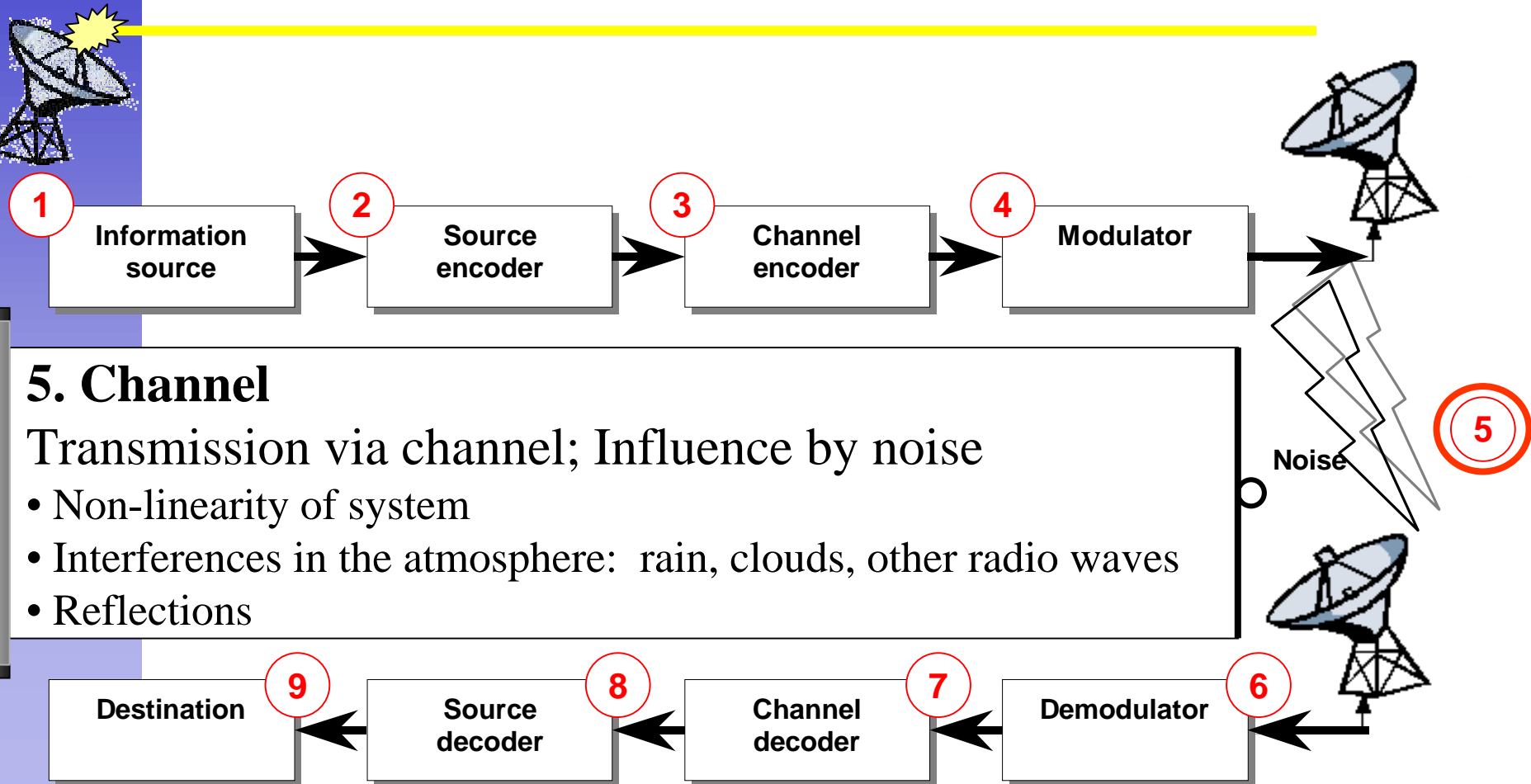
3. Channel encoder

- Transformation of information sequence into encoded sequence
- Adding of redundant information for error recognition and correction
=> Code word

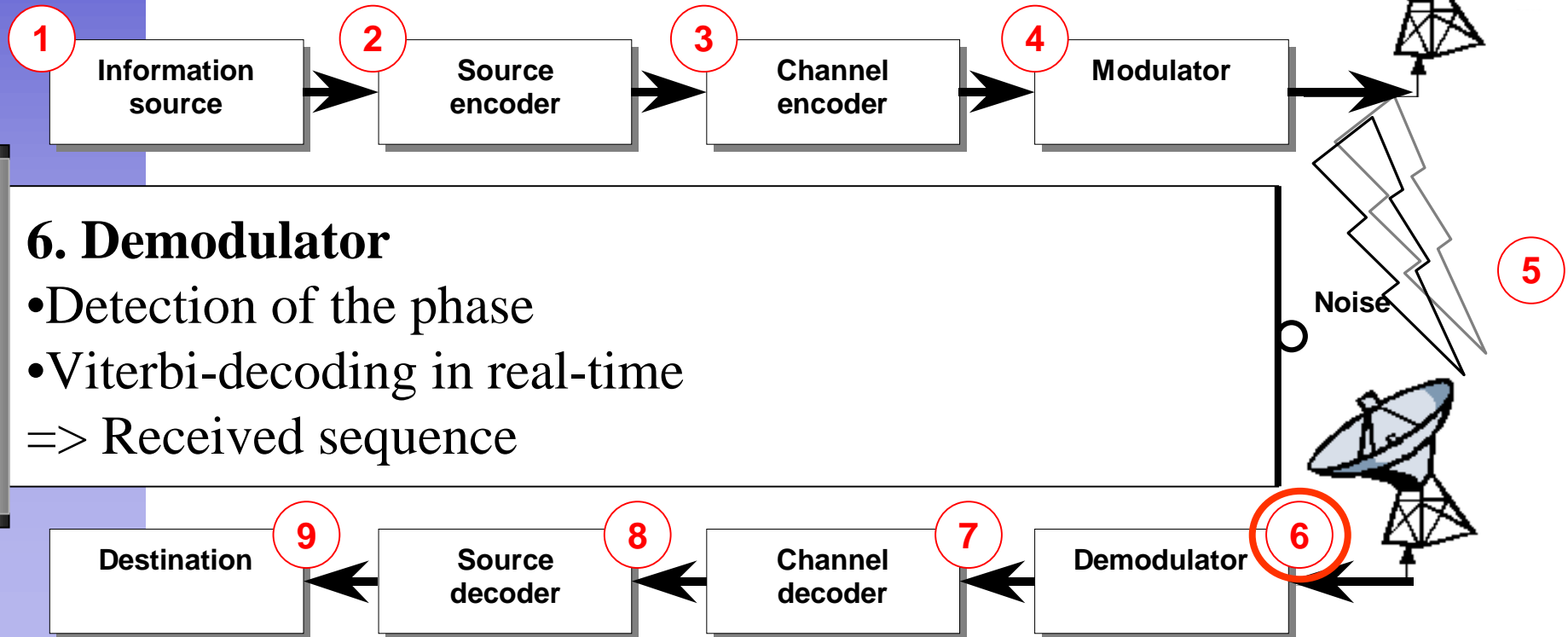
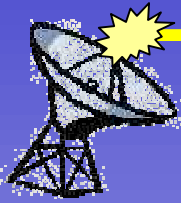
Digital communication system



Digital communication system



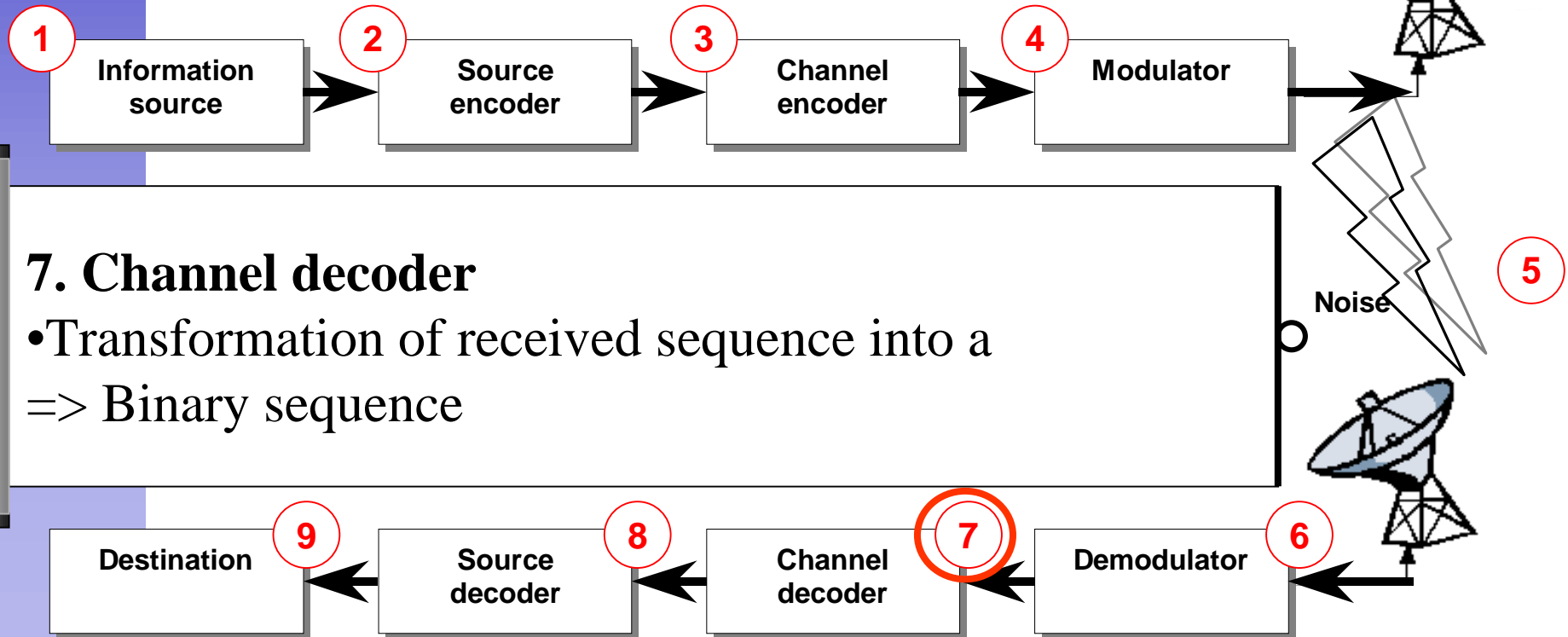
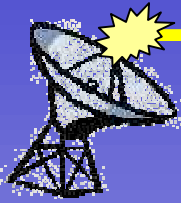
Digital communication system



6. Demodulator

- Detection of the phase
 - Viterbi-decoding in real-time
- ⇒ Received sequence

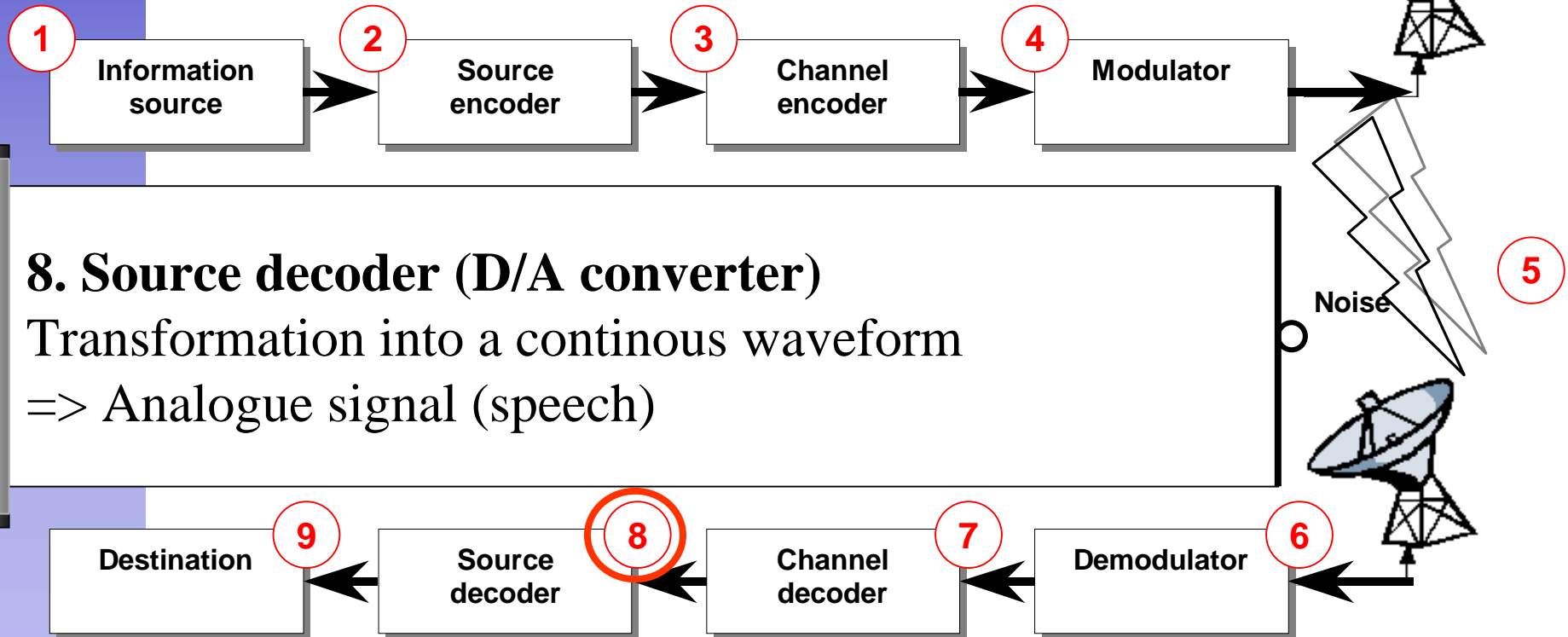
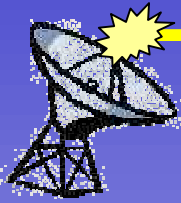
Digital communication system



7. Channel decoder

- Transformation of received sequence into a
=> Binary sequence

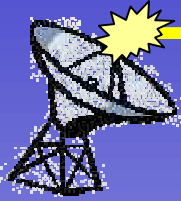
Digital communication system



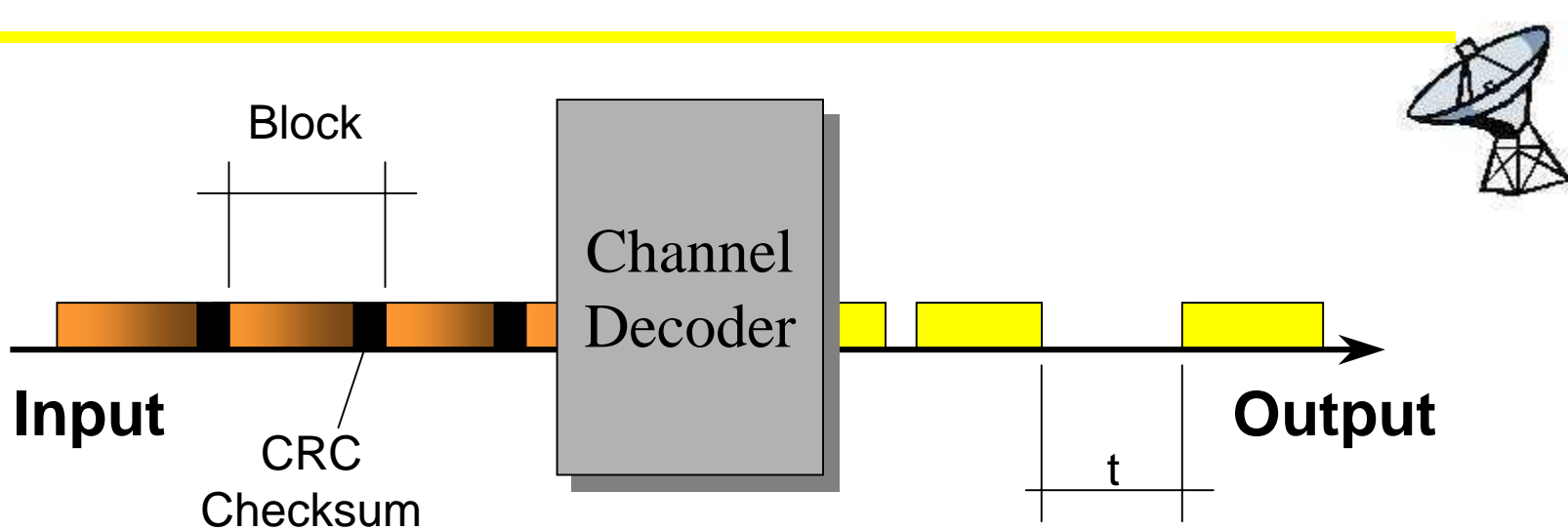
Channel coding: Code Types

Code Types:

- Block coding
- Convolutional coding



1. Block coding



- Input:
 - Large message blocks with CRC
- Output:
 - Block code with different length and breaks

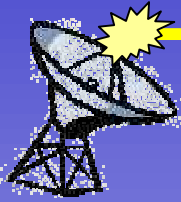
1. Block coding

Example of Block Coding:

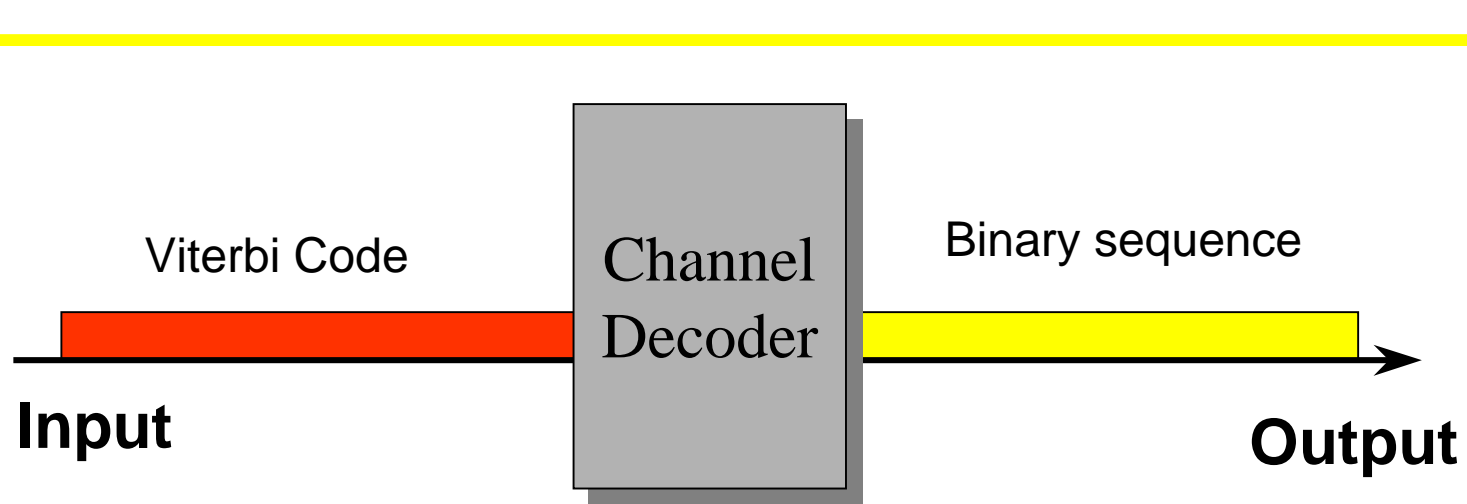
- Reed-Solomon Block:



- Recognition and correction of 8 error-bytes



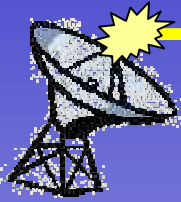
2. Convolutional Coding



- **Input:**
 - Serial data stream with includes redundant information
- **Output:**
 - Decoded binary data stream

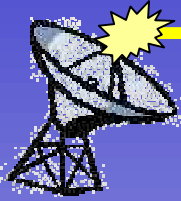
Use of the Viterbi Algorithm

- Low Signal to noise ratio ratio
- Radio link
- Satellite connection
- Digital TV (MPEG-2/DVB)
- Geostationary satellite networks (VSAT)
- Speech recognition
- Magnetic recoring
- Direct broadcast satellite systems (DBS)



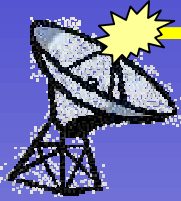
2. Description of the Algorithmus

- Generation of the data
- Convolutional encoder
- Parameters
- Channel symbols mapping
- Noise adding
- Channel symbol quantizing
- Viterbi Decoding

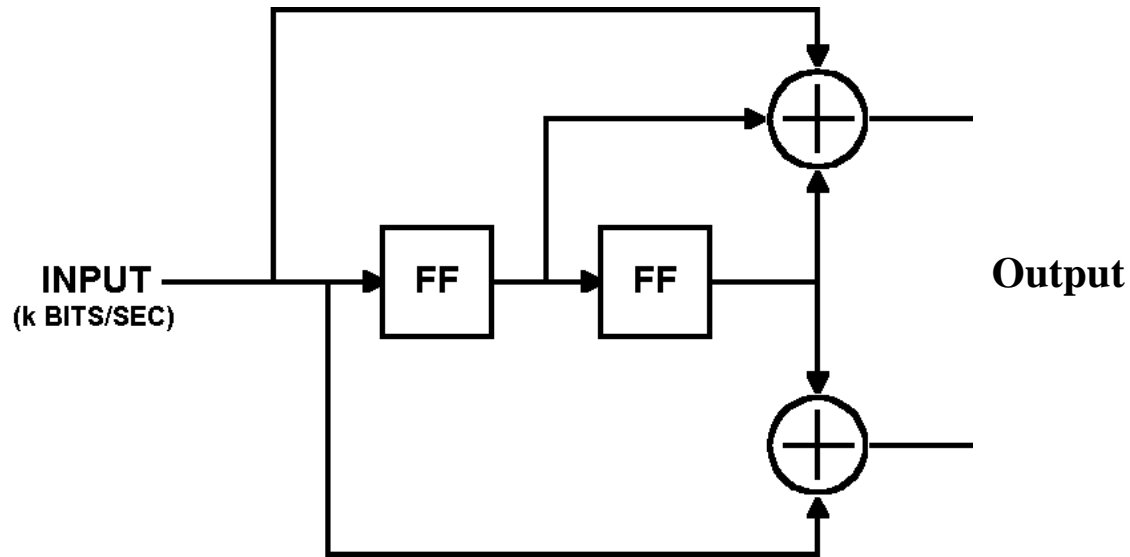
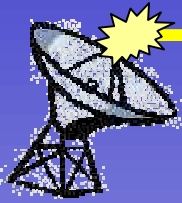


Generation of the data

- needed for simulation
- eg. using a random number generator
 - eg. `rand ()`; in C
 - value less than half of the maximum value is a zero
 - any value greater or equal to half of the maximum value is a one

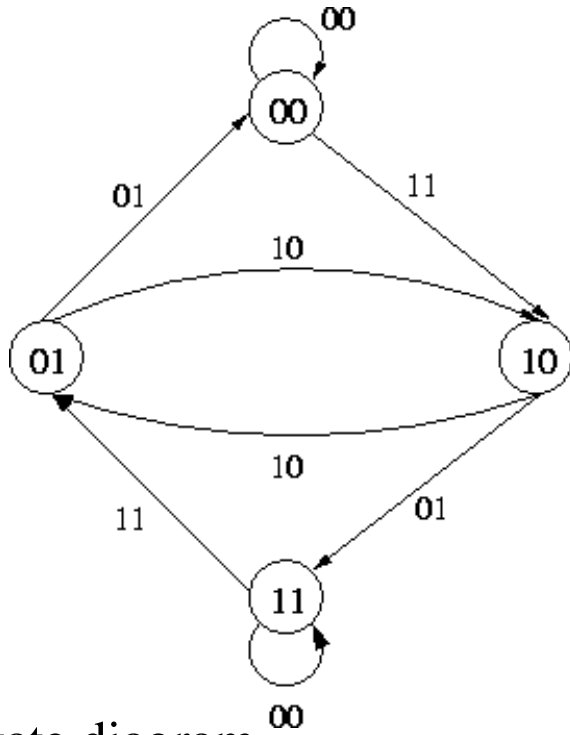


Convolutional encoder

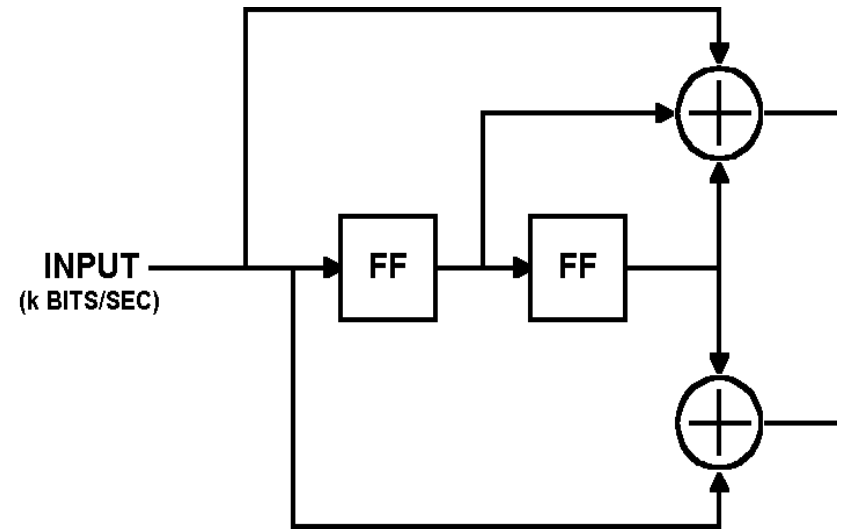


Convolutional encoder

2. Description of the Algorithm



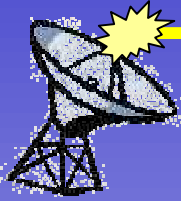
State diagram



Encoder

Parameters

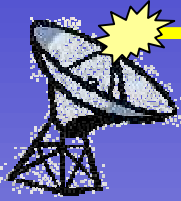
- eg. $k=3$
 - represent the code generator polynomials
- eg. $m=2$
 - number of shift-register
- eg. $R=1/2$
 - code rate (one inputbit \Rightarrow two outputbits)



Channel symbols mapping

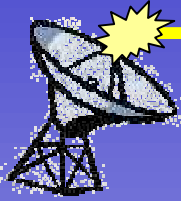
- Is simply a matter of translating:
 - zeros to +1
 - ones to -1
- method is called living zero

This can be accomplished by performing the operation: $y = 1-2x$



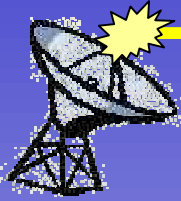
Noise adding

- generating Gaussian random numbers
- adding the scaled Gaussian random numbers to the channel symbols values



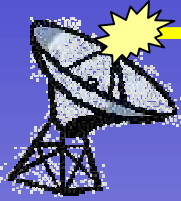
Channel symbol quantizing

- Hard-decision
- Soft-decision



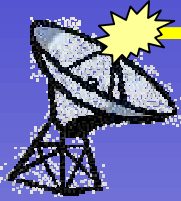
Hard-decision

- quantized to one-bit precision
 - $< 0V = 1$
 - $> 0V = 0$

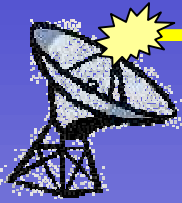
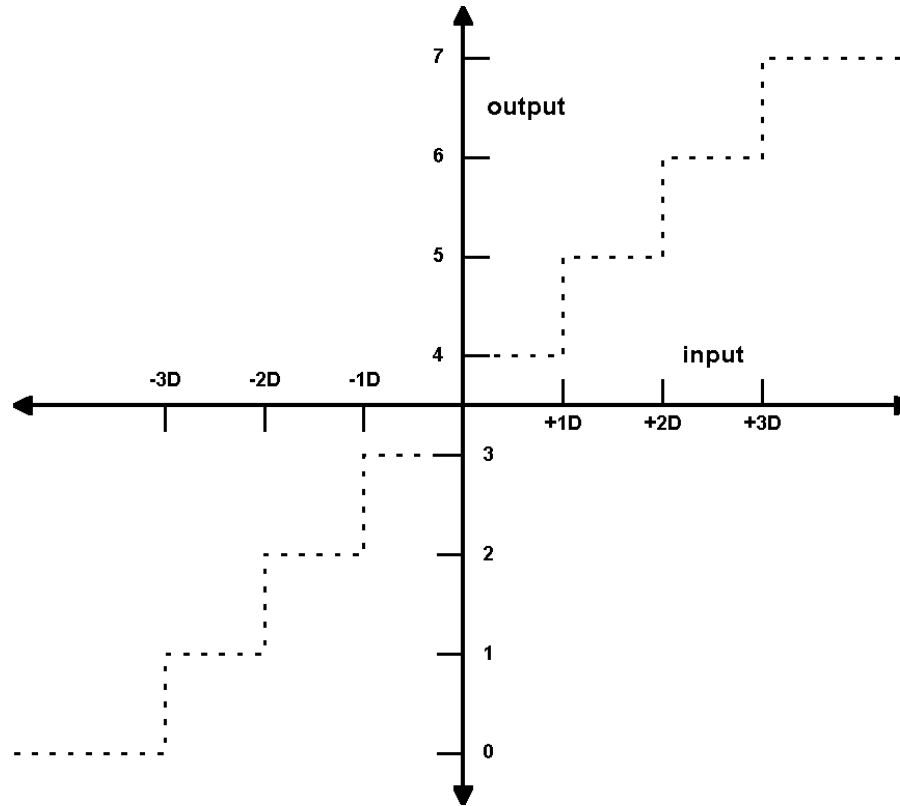


Soft-decision

- quantized with more than one bit of precision
- three or four bits of precision can perform about 2 dB better than hard-decision
- the usual quantization precision is three bits

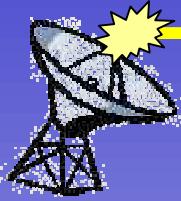


3 Bit Quantizer

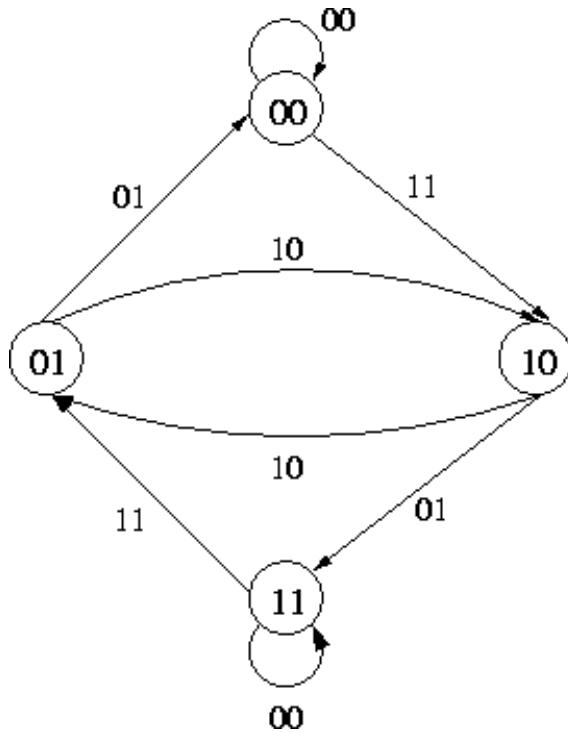
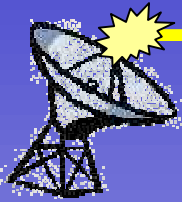


Viterbi Decoding

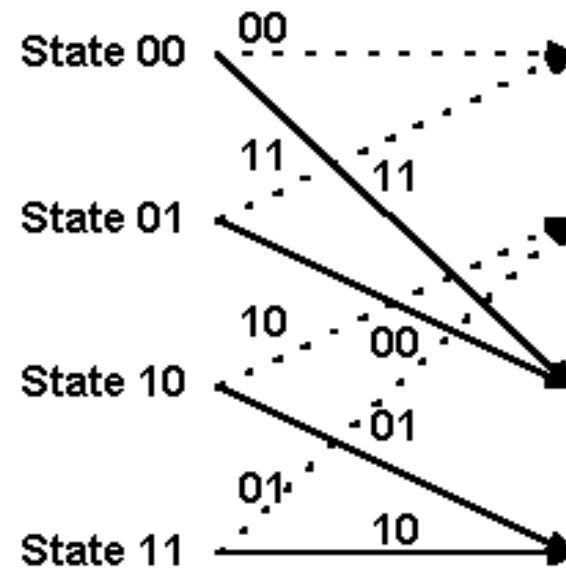
- Diagrams help to understand the algorithm
 - State diagram
 - Trellis diagram



State diagram / Trellis diagram

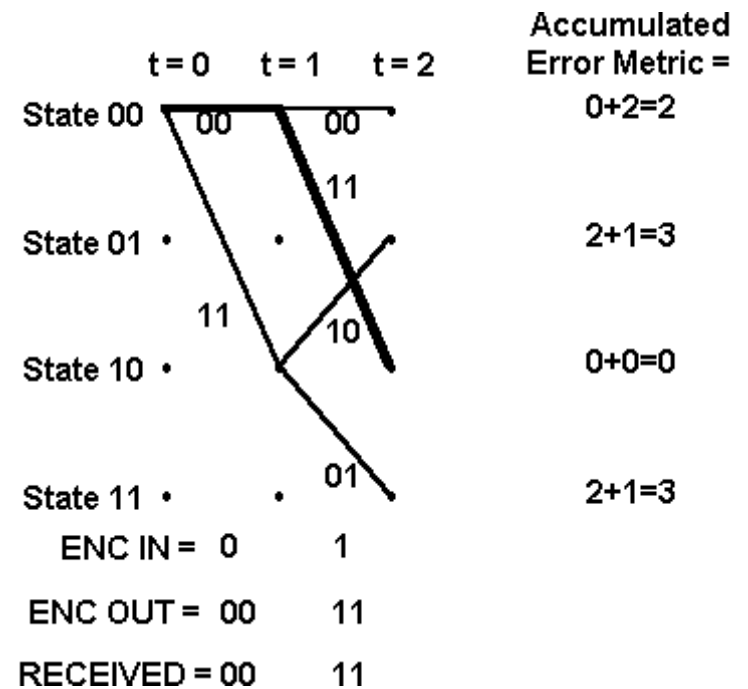
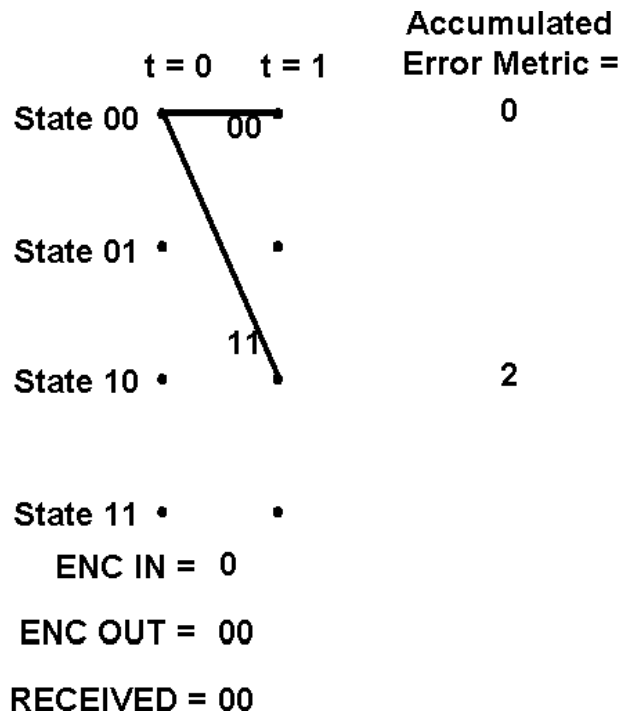
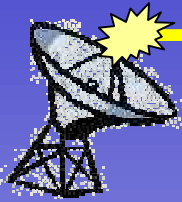


State diagram

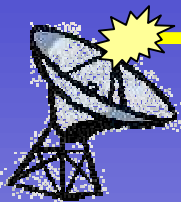


Trellis diagram

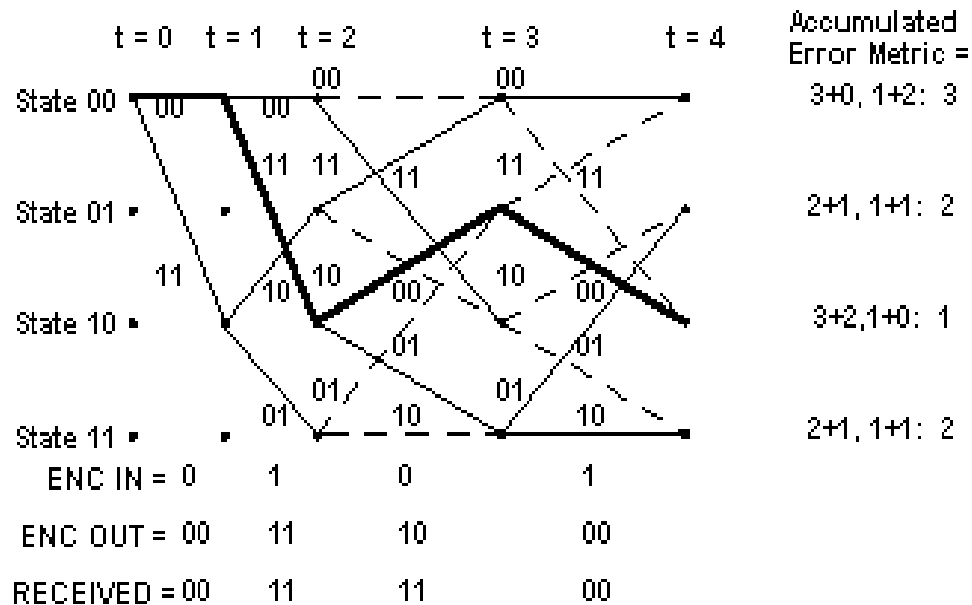
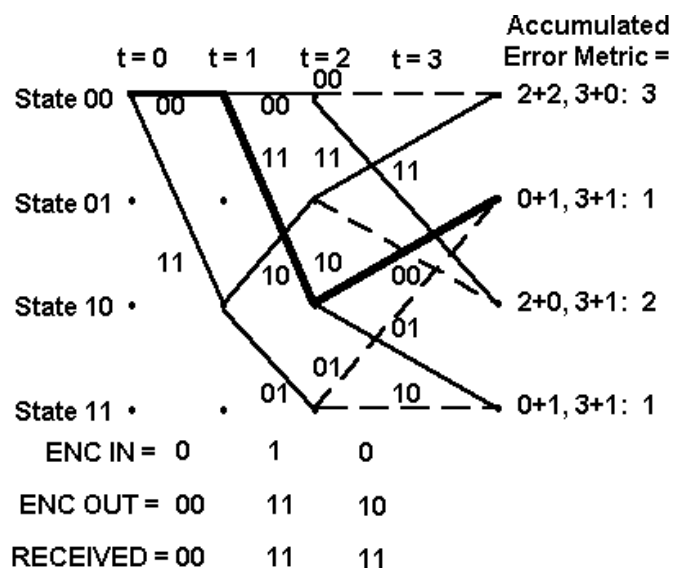
Viterbi decoding 1



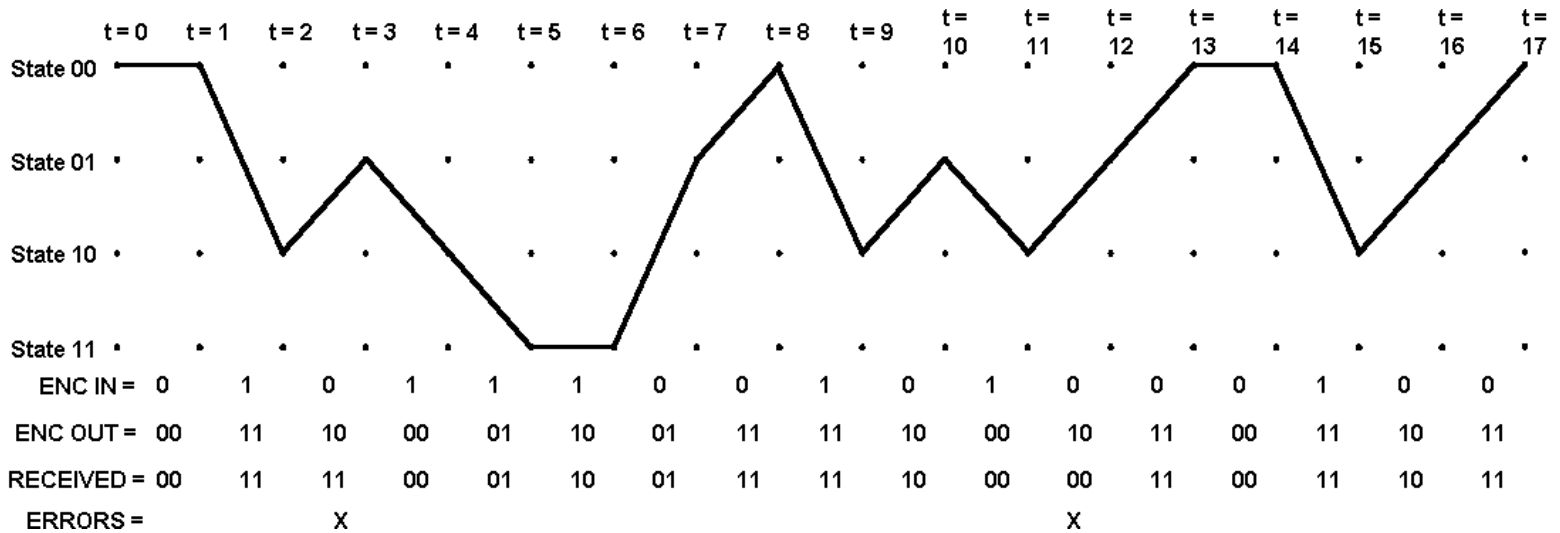
Viterbi decoding 2



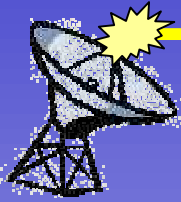
2. Description of the Algorithm



Trellis diagram

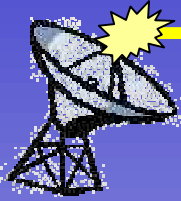


current	next	sended bit
00	00	0
00	10	1
10	01	0
10	11	1
01	00	0
01	10	1
11	01	0
11	11	1



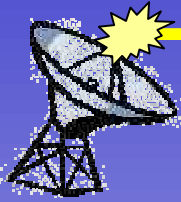
3. Advantages of the Viterbi Algorithm

- Self-Correction of the Code
- Minimization of the Transmitting Energy
- Minimization of the Bandwidth
- Other Advantages



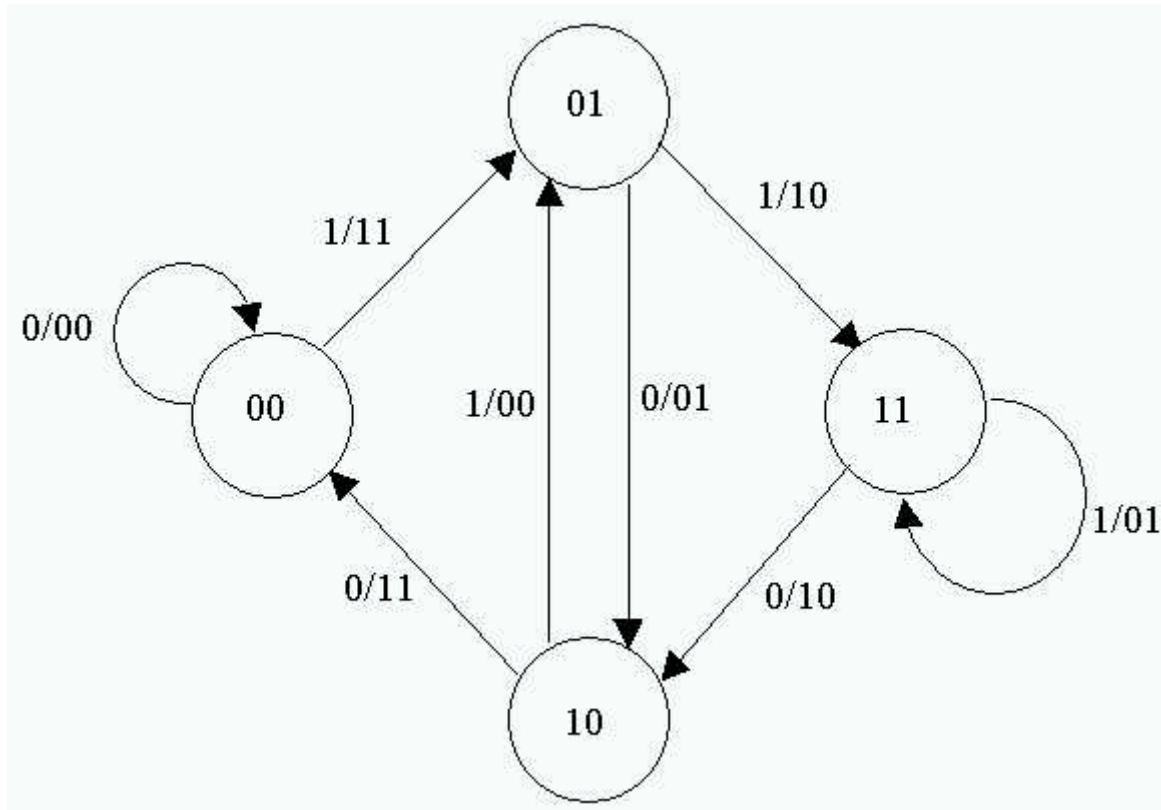
Self-Correction of the Code

- very good ability to correct wrong transmitted bits \Rightarrow forward error correction
- done by adding of a redundant information
- state diagram offers a complete description of the system



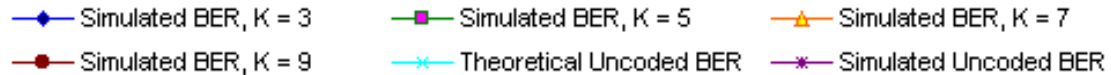
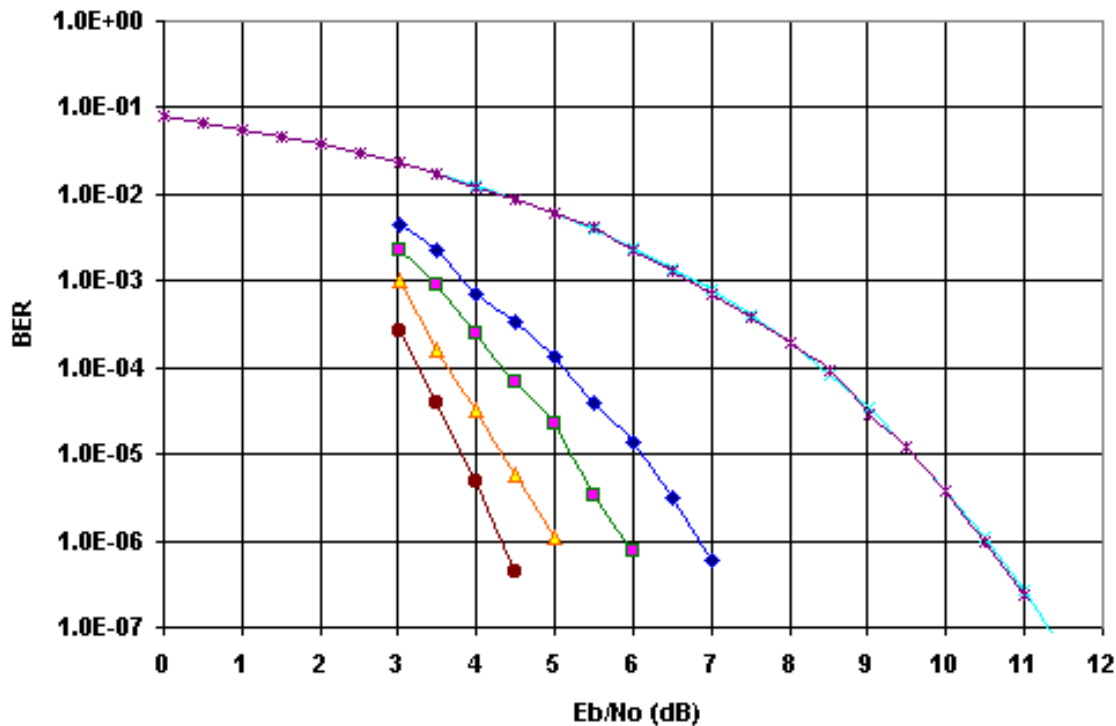
Self-Correction of the Code

- State diagram



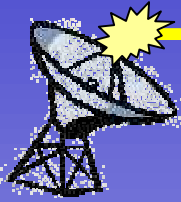
Minimization of the Transmitting Energy

- **BER** Simulation Results for Rate 1/2 Convolutional Coding with Viterbi Decoding on an AWGN Channel with Various Convolutional Code Constraint Lengths



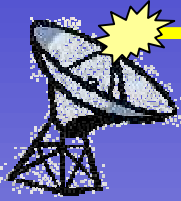
Minimization of the Transmitting Energy

- good designed satellite transmissions: $BER < 10^{-6}$
- professional transmissions: $BER < 10^{-10}$
- transmitting power: 4 Watt



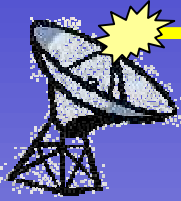
Minimization of the Bandwidth

- possible to reconstruct lost data \Rightarrow used to save bandwidth
- more bandwidth needed, because of all the redundant information
- rate $1/2 \Rightarrow$ double of the bandwidth
- don't send every third bit \Rightarrow able to reconstruct the dropped data



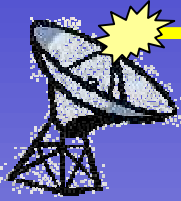
Minimization of the Bandwidth

- called puncturing of the code
- disadvantage: the transmitting energy have to be increased



Other Advantages

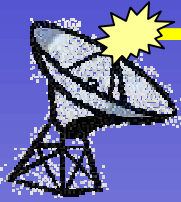
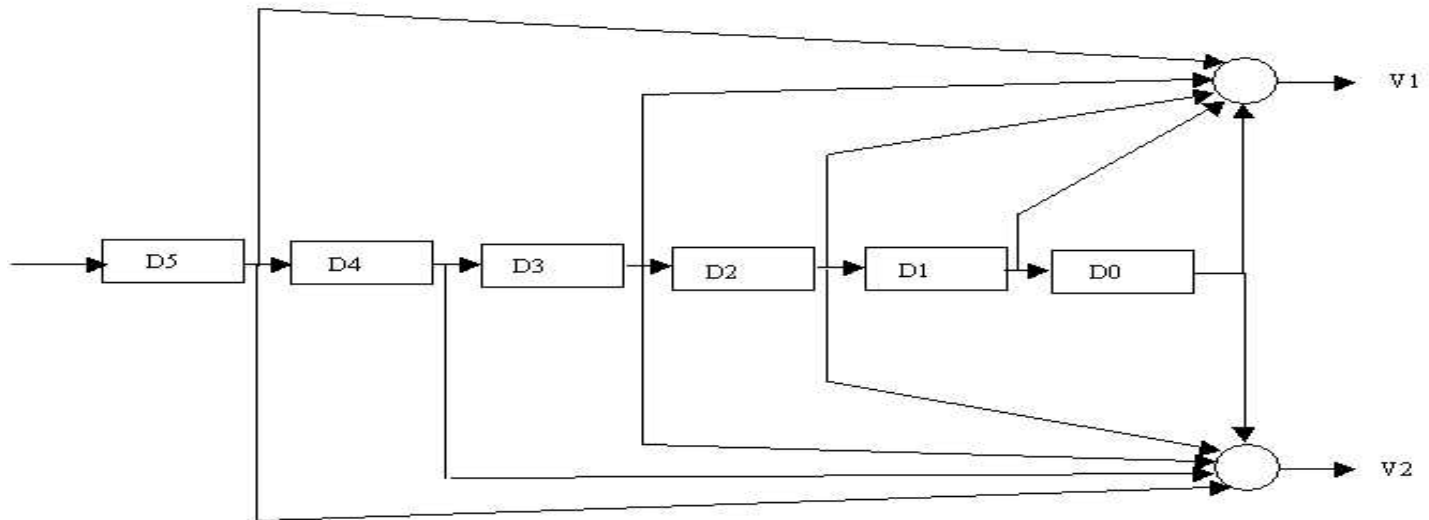
- fixed decoding time
- high transfer rate, up to 2 Mbps
- implementation in hardware and software

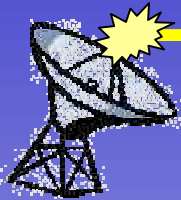


4. Presentation of the Software

- task:

- constraint length: 7
- code rate: 1/2
- soft decision: 3 bit quantizer





Viterbi Algorithm

Thank You for Your Attention!